

Early Journal Content on JSTOR, Free to Anyone in the World

This article is one of nearly 500,000 scholarly works digitized and made freely available to everyone in the world by JSTOR.

Known as the Early Journal Content, this set of works include research articles, news, letters, and other writings published in more than 200 of the oldest leading academic journals. The works date from the mid-seventeenth to the early twentieth centuries.

We encourage people to read and share the Early Journal Content openly and to tell others that this resource exists. People may post this content online or redistribute in any way for non-commercial purposes.

Read more about Early Journal Content at http://about.jstor.org/participate-jstor/individuals/early-journal-content.

JSTOR is a digital library of academic journals, books, and primary source objects. JSTOR helps people discover, use, and build upon a wide range of content through a powerful research and teaching platform, and preserves this content for future generations. JSTOR is part of ITHAKA, a not-for-profit organization that also includes Ithaka S+R and Portico. For more information about JSTOR, please contact support@jstor.org.

 $b'=\pm 1,\ b''=\pm 3$; and the four roots of C'=0 are, $x_3=1+\sqrt{-1},\ x_4=1-\sqrt{-1},\ x_5=-2+3\sqrt{-1},\ x_6=-2-3\sqrt{-1}.$ Therefore the seven roots of (1) are as follows:

$$\begin{array}{c} x_1=2,\ x_2=3,\ x_3=1+\sqrt{-1},\ x_4=1-\sqrt{-1}\\ x_5=-2+3\sqrt{-1},\ x_6=-2-3\sqrt{-1},\ x_7=-3+5\sqrt{1};\\ \mathrm{and}-(x_1+x_2+x_3+\ldots x_7)=A_1+B_1\sqrt{-1}=+(0-5\sqrt{-1});\\ -(x_1\cdot x_2\cdot x_3\ldots x_7)=A_{2^{n+1}}+B_{2^{n+1}}\sqrt{-1}=468-780\sqrt{-1}.\\ B.\ \ X=x^3-(7+5i)x_2+(19+30i)x-(13+65i)=0.\\ \mathrm{Here}\ \ N=-5x^2+30x-65=0,\ \mathrm{or}\ N=x^2-6x+13=0; \end{array}$$

Here
$$N = -5x^2 + 30x - 65 = 0$$
, or $N = x^2 - 6x + 13 = 0$; and $B_1 = b_{n+1} = +5$, $A_1 - B_2 \div B_1 = -a_{n+1} = -7 + 6 = -1$, $a_{n+1} \pm b_{n+1} \sqrt{-1} = 1 \pm 5\sqrt{-1}$.

X=0 is divisible by $[x-(1+5\sqrt{-1})]$ only, therefore $x^3=1+5\sqrt{-1}$ is a root of x=0, and we have $X\div(x-x_3)=N=0$.

Introducing in this equation x = a + bi, we get

$$N' \equiv a_1^2 - b_1^2 - 6a_1 + 13 + (2a_1b_1 - 6b_1)\sqrt{-1} = 0; \quad \text{and}$$

$$(A) \quad a_1^2 - b_1^2 - 6a_1 + 13 = 0, \quad (B) \quad 2a_1b_1 - 6b_1 = 0.$$

$$(B) \text{ gives } a_1 = 3, \text{ and } (A) \text{ gives } b_1 = \pm 2; \text{ therefore the roots of } N = 0$$

$$\text{are } x_1 = 3 + 2\sqrt{-1}, \ x_2 = 3 - 2\sqrt{-1}, \text{ and the three roots of } X = 0$$

$$\text{are } x_1 = 3 + 2\sqrt{-1}, \ x_2 = 3 - 2\sqrt{-1}, \ x_3 = 1 + 5\sqrt{-1}; \quad \text{and}$$

$$-(x_1 + x_2 + x_3) = -(7 + 5\sqrt{-1}) = A_1 + B_1\sqrt{-1},$$

$$-(x_1 \cdot x_2 \cdot x_3) = -(13 + 65\sqrt{-1}) = A_{2^{n+1}} + B_{3^{n+1}}\sqrt{-1}.$$

Note by Artemas Martin.—I have discovered that the formula given by me at the top of page 119, No. 7, Vol. I of the Analyst, holds only when n = 2.

Since the equation $\sqrt{a} = \frac{a}{r_m} \left[1 - \left(\frac{R_m}{a} \right) \right]^{\frac{1}{2}}$, where $R_m = a - r_m^2$, is identical, it should be written, to reduce r_m and R_m to integers,

$$\sqrt{a} = \frac{(10)^m a}{(10)^m r_m} \left[1 - \frac{(10)^{2m} \left(\frac{R_m}{a} \right)}{(10)^{2m}} \right]^{\frac{1}{2}}.$$

The formula for the nth root is

$$\sqrt[n]{a} = \frac{a}{r_m} \left[1 - \left(\frac{S_m}{a} \right) \right]^{\frac{1}{n}}, \text{ where } S_m = a^{n-1} - r_m^n;$$

but it does not appear to be of any practical use except when n=2.